

Correspondence Between Logic and Set Theory

<p>Logic</p> <p>Is a proposition A true?</p> <p>A is True</p> <p>A is False</p>	<p>Set Theory</p> <p>Is an object x in a set A?</p> <p>$x \in A$</p> <p>$x \notin A$</p>
<p>$\neg A$</p> <p>$A \vee B$</p> <p>$A \wedge B$</p> <p>$A \wedge \neg B$</p>	<p>\bar{A}</p> <p>$A \cup B$</p> <p>$A \cap B$</p> <p>$A \setminus B$</p>
<p>$A \rightarrow B$ is a tautology</p> <p>$A \leftrightarrow B$ is a tautology</p>	<p>$A \subseteq B$</p> <p>$A = B$</p>
<p>$A, B \vdash A \cap B$</p> <p>$A \cap B \vdash A$</p> <p>Modus ponens: $A, A \rightarrow B \vdash B$</p> <p>If we assume A and deduce B then $A \rightarrow B$.</p> <p>$A \vdash A \vee B$</p> <p>$A \vee B, A \rightarrow C, B \rightarrow C \vdash C$</p> <p>$\perp \vdash A$</p>	<p>If $x \in A$ and $x \in B$ then $x \in A \cap B$</p> <p>If $x \in A \cap B$ then $x \in A$</p> <p>If $x \in A$ and $A \subseteq B$ then $x \in B$.</p> <p>If we can take an arbitrary $x \in A$ and show that $x \in B$ then $A \subseteq B$.</p> <p>If $x \in A$ then $x \in A \cup B$</p> <p>If $x \in A \cup B, A \subseteq C, \text{ and } B \subseteq C$ then $x \in C$.</p> <p>For any set $A, \emptyset \subseteq A$</p>
<p>True</p> <p>False</p>	<p>Universe U</p> <p>\emptyset</p>

Correspondence Between Logic and Set Theory

Logic

Set Theory

Distributive Laws:
 $A \wedge (B \vee C) \leftrightarrow (A \wedge B) \vee (A \wedge C)$
 $A \vee (B \wedge C) \leftrightarrow (A \vee B) \wedge (A \vee C)$

$A \cap (B \cup C) = (A \cap B) \cup (A \cap C)$
 $A \cup (B \cap C) = (A \cup B) \cap (A \cup C)$

De Morgan's Laws:
 $\neg(A \vee B) \leftrightarrow \neg A \wedge \neg B$
 $\neg(A \wedge B) \leftrightarrow \neg A \vee \neg B$

$\overline{A \cup B} = \bar{A} \cap \bar{B}$
 $\overline{A \cap B} = \bar{A} \cup \bar{B}$

\rightarrow is transitive. $A \rightarrow B, B \rightarrow C \vdash A \rightarrow C$

\subseteq is transitive. If $A \subseteq B$ and $B \subseteq C$ then $A \subseteq C$.

Law of the Excluded Middle: $A \vee \neg A$
 Principle of Double Negation: $\neg\neg A \leftrightarrow A$
 Law of Contraposition: $A \rightarrow B \leftrightarrow \neg B \rightarrow \neg A$

For any object x and set A , either $x \in A$ or $x \notin A$.

$$\overline{\bar{A}} = A$$

$A \subseteq B$ if and only if $\bar{B} \subseteq \bar{A}$